

Progression of skills

Addition and Subtraction

How do we teach Mathematics at St Catherine's?

- White Rose Maths
- Follow a CPA approach
- Children engaging in appropriate, cognitively-challenging activities - practical and experiential learning activities.
- A culture that supports children's curiosity, thinking and problem solving

- Modelling/ guided and independent practice My turn your turn/ I do, we do, you do approach.
- Flashback 4 Starter activities encourage children to know more and remember more– Recap of learning yesterday, last week, last topic, last half term. – Making links
- Vocabulary/ full sentence answers- embodies and communicates concepts, emphasis on key vocabulary.

What is Place Value?

Place value is the value of each digit in a number. Eg:

350- the 5 represents 5 tens, or 50. 5,006- the five represents thousands or 5,000.

- It is important that children understand that whilst a digit can be the same, its value depends on where it is in the number.
- Place value is one of the most important areas of the primary maths curriculum.

Ten Millions	Millions	Hundred	Ten Thousands	Thousands	Hundreds	Tens	Ones

How to use a place value chart: 1,708 27,085

Ten Millions	Millions	Hundred Thousands	Ten Thousands	Thousands	Hundreds	Tens	Ones
				1	7	0	8
			2	7	0	8	5

Mathematics in the EYFS

Number

- Recognise, count and order numbers up to 20
- Finding one more or one less than a given number.
- Add and subtract two single-digit numbers and count on or back to find the answer. E.g. 2 + 5=
- Solve problems, including doubling, halving and sharing.

Year 1-6

- Place Value:
- Counting
- Represent
- Comparing
- Problems

Place Value in Year 1

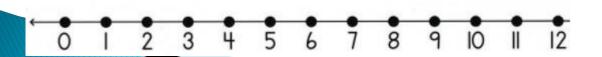
Count to and across 100, forwards and backwards beginning with 0 or 1, or from any given number;

Count, read and write numbers to 100 in numerals;

Count in multiples of twos, fives and tens using a

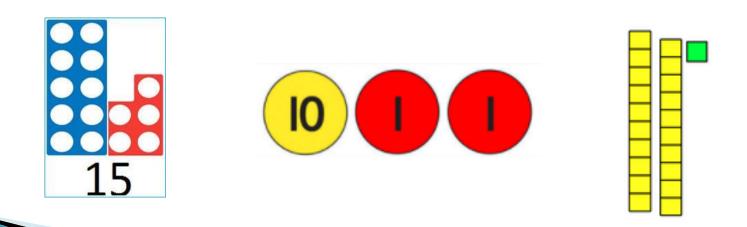
100 square, coins;

Identifying one more and one less.E.g splat square, number line



1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

- Identify and represent numbers using objects and pictorial representations;
- Using language of equal to and more than, less than (fewer);
- Read and write numbers from 1 to 20 in numerals and words.



Place Value in Year 2

> Count in steps of 2, 3 and 5 from 0, and in tens from any number forward and backwards.

E.g. 30, 40, 50 2, 4, 6, 8 21, 24, 27 15, 10, 5

2		8		14

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30

Read and write numbers to at least 100 in numerals and words;

Numerals	Number in Words	Tens	Ones	Illustration
23	twenty-three	2	3	

➤ Identify, represent and estimate numbers using different representations including a number line;

Represent the following number on a 0-100 number line.



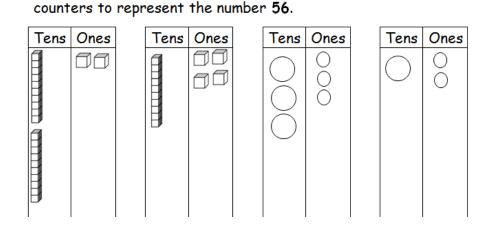
0 100

Recognise the place value of each digit in a two-digit number (tens, ones);

Number	Bui	ld	
		a	

Number	Build
5	

- Compare and order numbers from 0 up to 100; use <, > and = signs. E.g. 6=6 6<18</p>
- ➤ Use place value and number facts to solve problems; Complete the place value charts using Base 10 and place value



By the end of year 2, pupils should know the number bonds to 20 and be precise in using and understanding place value.

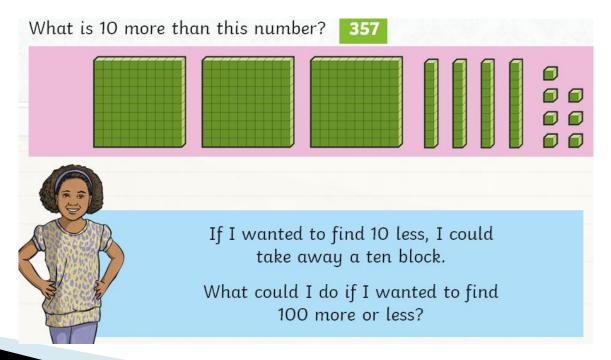
E.g.
$$10+8=18$$
 $18-10=8$ $8+10=18$ $18-8=10$

Place Value in Year 3

Count from 0 in multiples of 4,8,50 and 100. E.g. can you count up to 80 using jumps of 4.

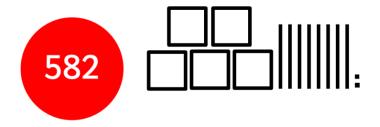
> Find 10 or 100 more or less than a given

number.



Identify, represent and estimate numbers using different representations.

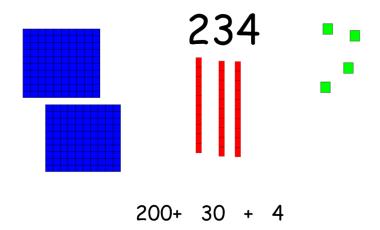
REPRESENTING NUMBERS BY DRAWING BASE 10



Recognise the place value of each digit in a three-digit number (hundreds, tens, ones)

Hundreds	Tens	Ones
2	4	1
200	40	1
	Î	1
The value of the 2 is 200	The value of the 4 is 40	The value of the 1 is 1

- > Compare and order numbers up to 1000.
- Read and write numbers to 1000 in numerals and in words.
- Use larger numbers to at least 1000, applying partitioning related to place value.

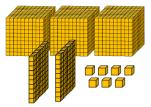


 Continue to count in ones, tens and hundreds, so that they become fluent in the order and place value of numbers to 1000.

Place Value in Year 4

- Count in multiples of 6, 7, 9, 25 and 1000. E.g. can you count up in 7s from 15.
- > Find 1000 more or less than a given number. E.g. what is 1000 less than 1532.
- Count backwards through zero to include negative numbers.

Identify, represent and estimate numbers using different 3207 representations.



REPRESENTING NUMBERS BY DRAWING BASE 10

Represent the following number by drawing base 10:

- 1468
- Recognise the place value of each digit in a four-digit number (thousands, hundreds, tens, and ones);
- Order and compare numbers beyond 1000. E.g. which number has the greatest value: **234.**5 or 1234.59

There are thousands, hundreds, tens and ones.
The number is
++=

Complete the part-whole model for the number represented.



What is the value of the underlined digit in each number?

6,9 <u>8</u> 3 <u>9</u> ,021 <u>7</u> 89 6,57 <u>0</u>	6,9 <u>8</u> 3	<u>9</u> ,021	<u>7</u> 89	6,57 <u>0</u>
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Represent each of the numbers on a place value grid.

> Round any number to the nearest 10, 100 or 1000.

Round 1289 to the nearest ten.

First, look at the ones digit:

128<u>9</u>

9 is greater than 5, so you **round up**.

So 1289 rounded to the nearest ten is <u>1290</u>.

The number line below also shows you how much closer 1289 is to 1290.



> Read Roman numerals to 100 (I to C).

$$I = 1$$

$$V = 5$$

$$X = 10$$

$$L=50$$

$$C = 100$$

Place Value in Year 5

Read, write, order and compare numbers to at least 1,000,000 and determine the value of each digit.

Order these numbers from smallest to largest:

34,111 1,142 2,466 321 3,232 5,542

Compare these numbers using symbols <>

Count forwards or backwards in steps of powers of 10 and for any given number up to 1,000,000. E.g. counting in groups of/ lots of 10 from any given number.

- Round any number up to 1,000,000 to the nearest 10, 100, 1000, 10 000 and 100 000.
- Read Roman numerals to 1000 (M) and recognise years written in Roman numerals.

 2009 MMIX

 2020 MMXX

Count forwards and backwards with positive and negative whole numbers, including through zero.
Start at 4. Count back 8.
What number do you reach? -4

2021 MMXXI

2022 MMXXII



Place Value in Year 6

> Read, write, order and compare numbers to 10,000,000 and determine the value of each digit.

	Millions	Hundred thousands	Ten thousands	Thousands	Hundreds	Tens	Units
816 958		8	1	6	9	5	8

- Order numbers with a different number of digits. E.g 10,245,000 945,000 459,250
- Round any whole number to a require degree of accuracy. E.g. 456 round to

$$1000=0$$
 $100=500$
 $10=460$

Use negative numbers in context, and calculate intervals across zero (temperature, money).

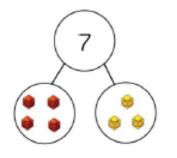
Month	J	F	М	Α	М	J	J	Α	S	0	N	D
Moscow- Average Temperatures ⁰ C	-8	-9	-3	5	11	19	23	21	10	4	-2	-6
Reykjavik Average Temperatures ⁰ C	2	2	1	1	4	7	9	8	6	3	0	2
Bournemouth Average Temperatures ⁰ C	4	5	8	10	11	15	18	17	14	12	7	5

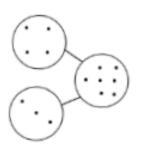
What is the difference between the coldest and warmest temperatures in <u>Moscow?</u>

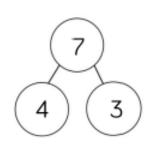
Addition and Subtraction

- Recall, Represent and Use
- Calculations
- Solve problems

Part-whole model





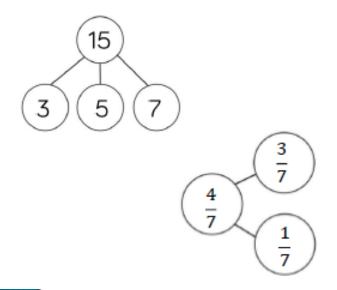


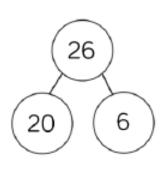
$$7 = 4 + 3$$

$$7 - 3 = 4$$

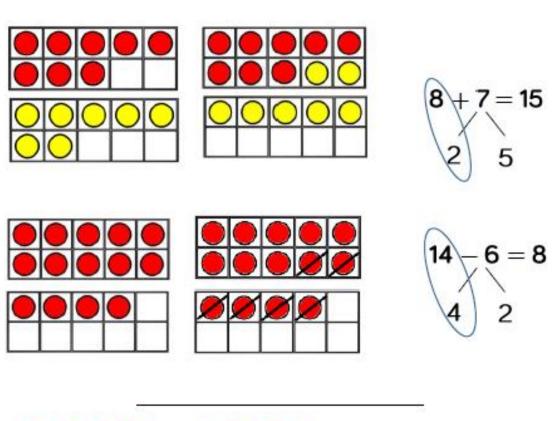
$$7 = 3 + 4$$

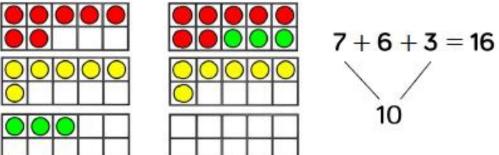
$$7 - 4 = 3$$



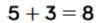


- Supports children's understanding of partitioning.
- When the parts are complete children add the parts together to find the total.
- When the whole is complete and at least one of the parts is empty, children use partitioning (a form of subtraction) to find the missing part.
- KS2 apply their understanding of the partwhole model to add and subtract fractions, decimals and percentages.





Support the link to effective mental methods of addition as well as the importance of commutativity.

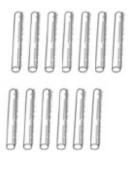


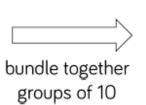
					Y	Y	1		
1	2	3	4	(5)	6	7	8	9	10

$$10 - 4 = 6$$

						1	Y	A	
1	2	3	4	5	6	7	8	9	10

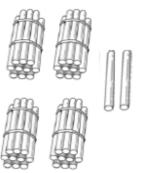
$$7 + 6 = 13$$

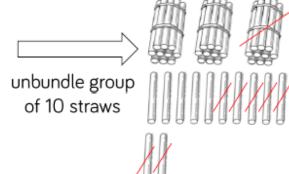






$$42 - 17 = 25$$





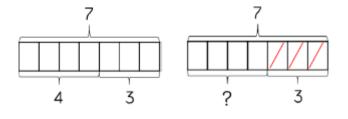
Bar Models

Concrete





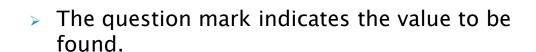
Supports children in representing calculations to help them unpick the structure.

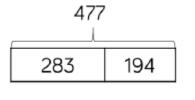


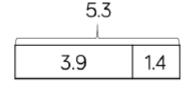
Cubes and counters can be used as concrete representations of the bar model.



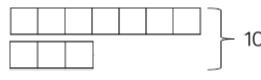
Support children to calculate by counting on from the larger number.







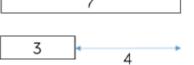
In KS2, children can use bar models to represent larger numbers, decimals and fractions.



$$7 + 3 = 10$$



$$7 - 3 = 4$$





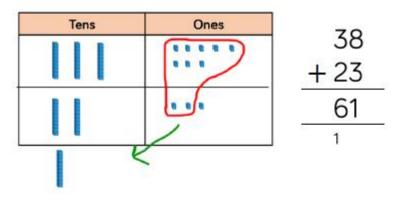
2,394

$$7 - 3 = 4$$

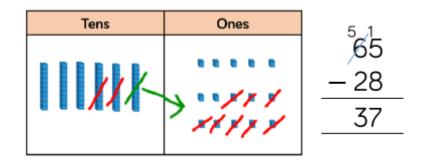
$$2,394 - 1,014 = 1,380$$

Base 10/ Dienes

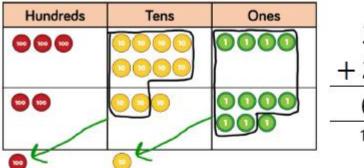
- Supports children's understanding of column addition.
- Important that children write out their calculations alongside using or drawing Base 10 so they can see the clear links between the written method and the model.
- Start adding without an exchange. The move in to addition with exchange.
- Less efficient with larger numbers-> Place value counters.
 - Adding always starts with the smallest place value column.

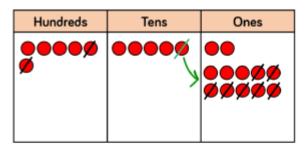


Hundreds	Tens	Ones	
			265
			+ 164
			429
			1



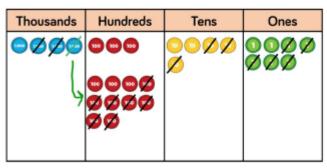
Place value counters





Ones	Tenths	Hundredths
	Q1 Q1 Q1	0.01 0.01 0.01
	(1) (1)	001 001
	01 01 01	0.01
00	(a)	

$$\begin{array}{r}
 3.65 \\
 + 2.41 \\
 \hline
 6.06 \\
 \end{array}$$



 $\frac{{}^{3}\cancel{4}^{1}}{357}$ $\frac{-2735}{1622}$

Addition and Subtraction

Year 1

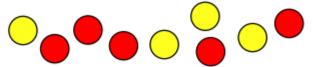




Read, write and interpret mathematical statements involving addition, subtraction and equals signs. E.g.

$$_{-} = 5 + 4$$

Represent and use number bonds and related subtraction facts within 20. Here are some counters.

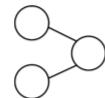


Group the counters by colour.

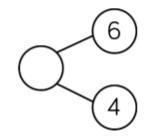
Fill in the gaps in the sentence and say it out loud.

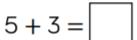
_____ red counters plus _____ yellow counters is equal to ____ counters.

Complete the part-whole model and the number sentence.



Use cubes to solve the following calculations.





Write the number fact to match the story and picture.

Star cooked 8 muffins. She gave 4 to her friend. How many muffins did Star have left?



Add and subtract one-digit and two-digit numbers to 20, including zero. E.g.

$$5-3=$$
 $12-6=$ $20 =$ 20

Solve one-step problems that involve addition and subtraction, using concrete objects and pictorial representations, and missing number problems such as

$$7 = ? - 9$$

E.g. Tony has 3 apples and Terry has 2 apples, How many altogether?

True or False?

If I add 0 to a number, the number stays the same.

Can you use a number line or counters to help you explain your answer?

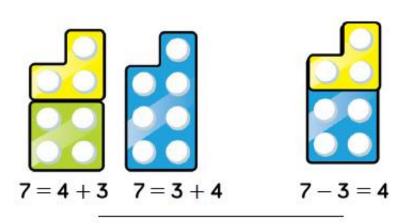
Mo has used the number track to complete 4 + 2
He thinks the total is 5





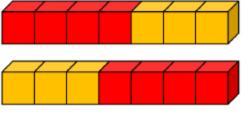
What mistake has he made? How could Mo use the number track to find the correct answer?

Numicon



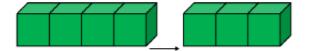
- Support children to subitise numbers as they become familiar with the shape of each number.
- Explore aggregation (form of addition where parts are combined together to make a whole), partitioning and number bonds.
- 6+4 7+3 8+2 9+1
- Subtraction children start with the whole and then place the parts on top to see what part is missing.
- Number bonds as you increase one number by 1, you can see that the other number decreases by 1 to find all the possible number bonds for a number.

Unifix cubes

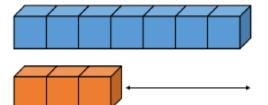


$$7 = 4 + 3$$





$$7 - 3 = 4$$

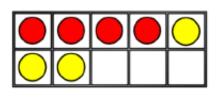


$$7 - 3 = 4$$

- Supports children with addition and subtraction of 1 digit numbers.
- Addition- Children can see how the parts come together to make a whole.
- Subtraction Start with the whole then removing the number of cubes being subtracted in order to find the answer.
- > Looking at subtraction as difference. Both numbers made and then lined up to find the different between the numbers.

Cubes work with smaller numbers as it is difficult to subitise with larger numbers and shildren may miscount them.

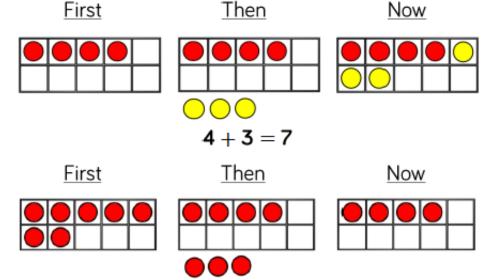
Ten Frames (within 10 and 20)



$$4+3=7$$
 4 is a part.
 $3+4=7$ 3 is a part.

7-3=4 7 is the whole. 7-4=3 Used for addition and subtraction.

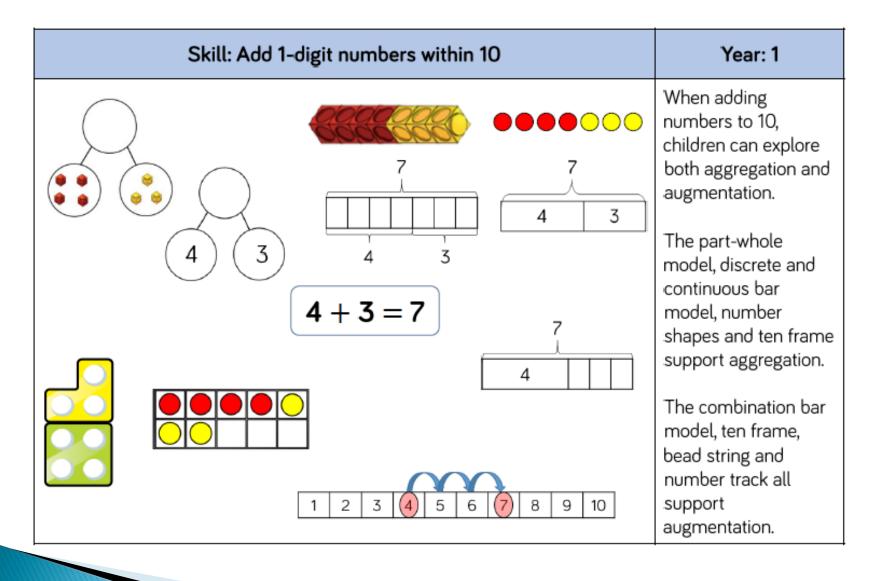
7 is the whole. > Support children to understand the different structures of addition and subtraction.



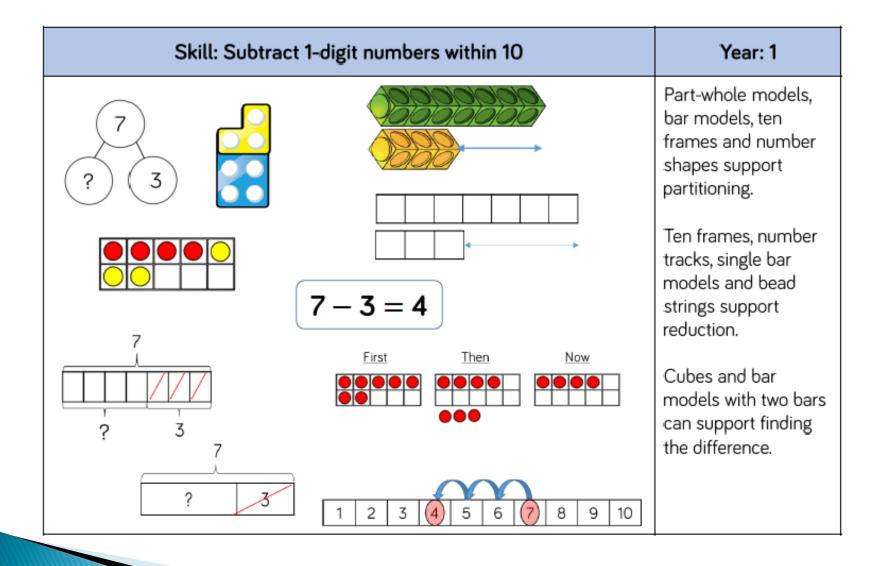
7 - 3 = 4

- Introduces children to aggregation and partitioning (whole is split into parts).
- Supports children to find all the number bonds for a number.
- Story structures Now, then, next. E.g. First there were 7 cars. Then, 3 cars left. Now, there are 4 cars.

Addition



Subtraction



Year 2

- Add and subtract numbers using concrete objects, pictorial representations, and mentally, including:
- A two-digit number and ones
- A two-digit number and tens
- Two two-digit numbers
- Adding three one-digit numbers

Use the place value charts and concrete materials to complete the calculations.

Tens	Ones
	25

2	3
+4	0

Tens	Ones

- Solve problems using concrete objects and pictorial representations and those involving numbers, quantities and measures. E.g. cubes, coins, measuring jugs of different amounts of ml.
- Recall and use addition and subtraction facts to 20 fluently, and derive and use related facts up to 100.

E.g.
$$4 + 6 = 40 + 60 =$$

$$9+1=10$$

 $19+1=20$

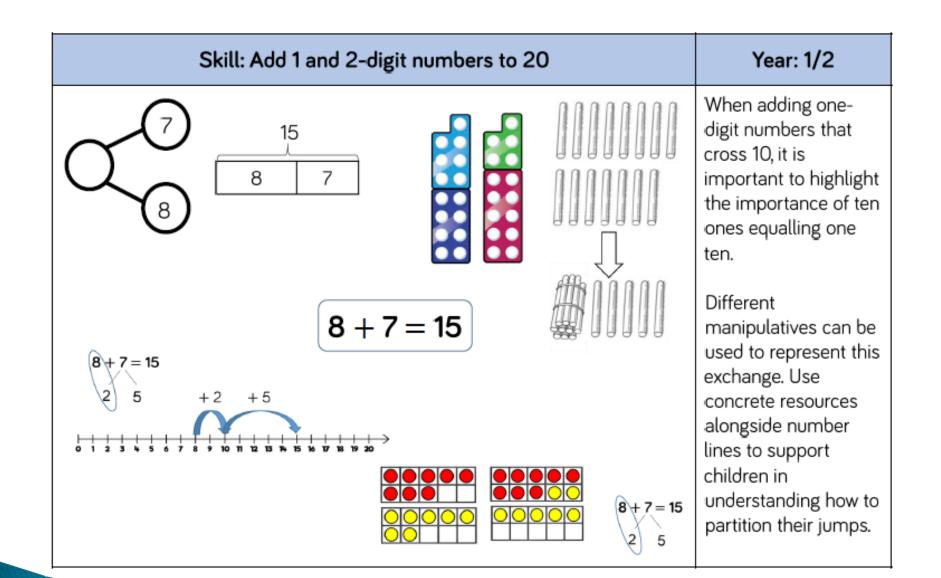
Show that addition of two numbers can be done in any order (commutative) and subtraction from another cannot. Recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems.

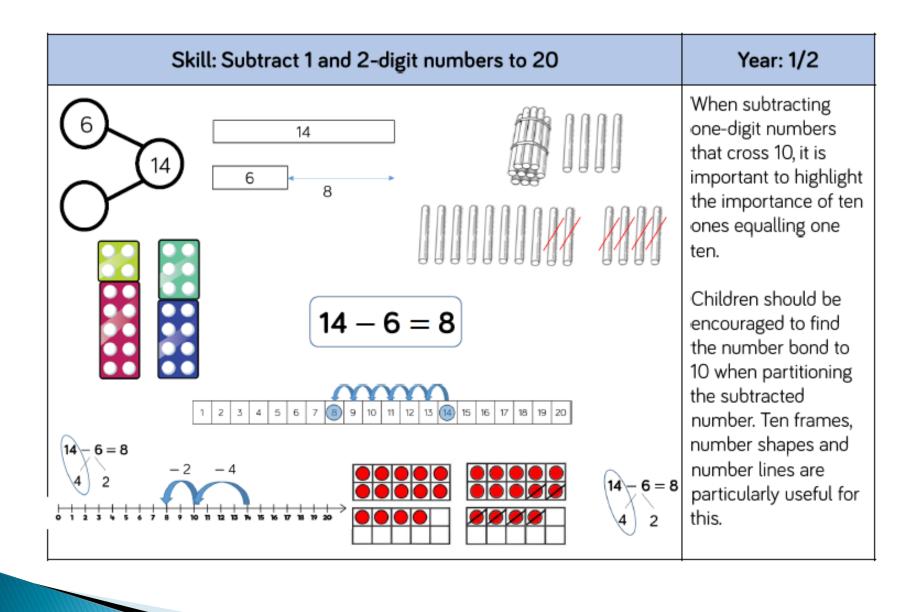
Can you use inverse operations to check 5 + 12 = 17?

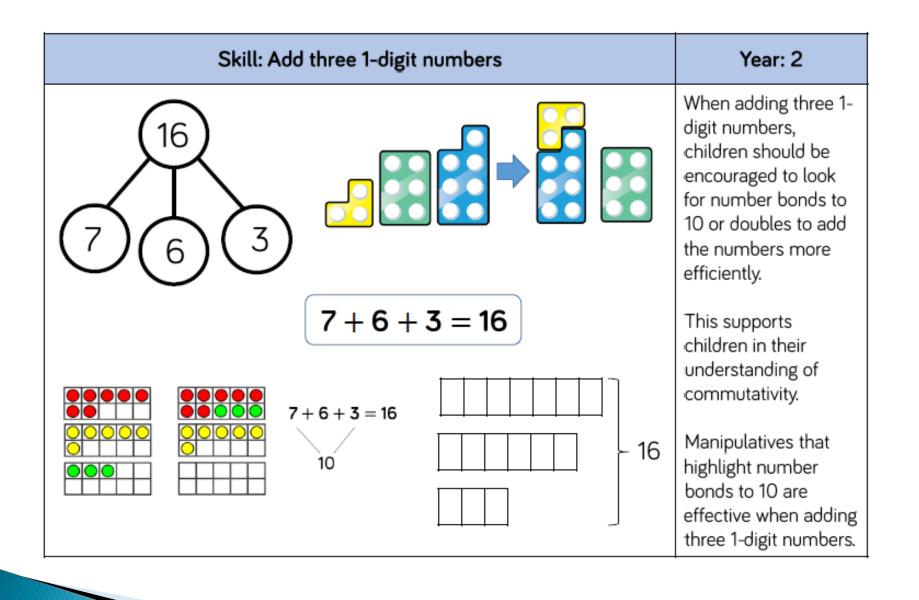
17	
12	5

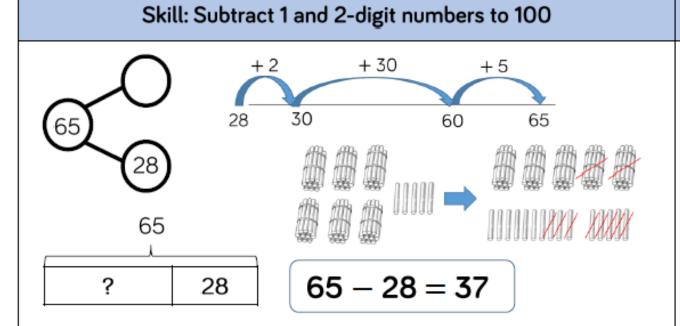
How many possible inverse calculations are there?

Eva writes this calculation: 18 - 5 = 13Which of the following could she use to check her work?









⁵65

28

37

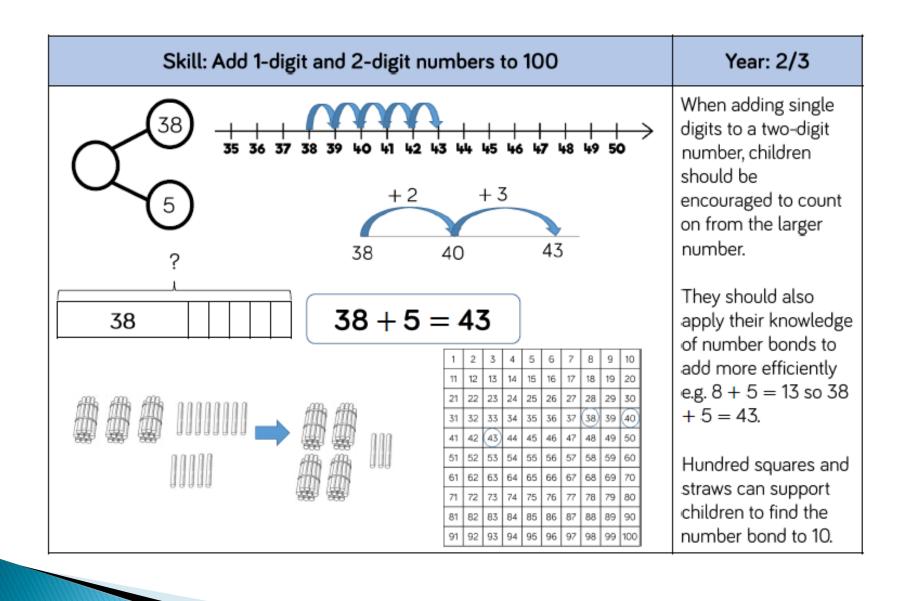
Tens	Ones
000	00000
Ø Ø Ø	
7	000000
	ØØØØØ

At this stage, encourage children to use the formal column method when calculating alongside straws, base 10 or place value counters. As numbers become larger, straws become less efficient.

Year: 2

Children can also use a blank number line to count on to find the difference.
Encourage them to jump to multiples of 10 to become more efficient.

Tens	Ones
/// /	711/14
	XXXX



Year 3

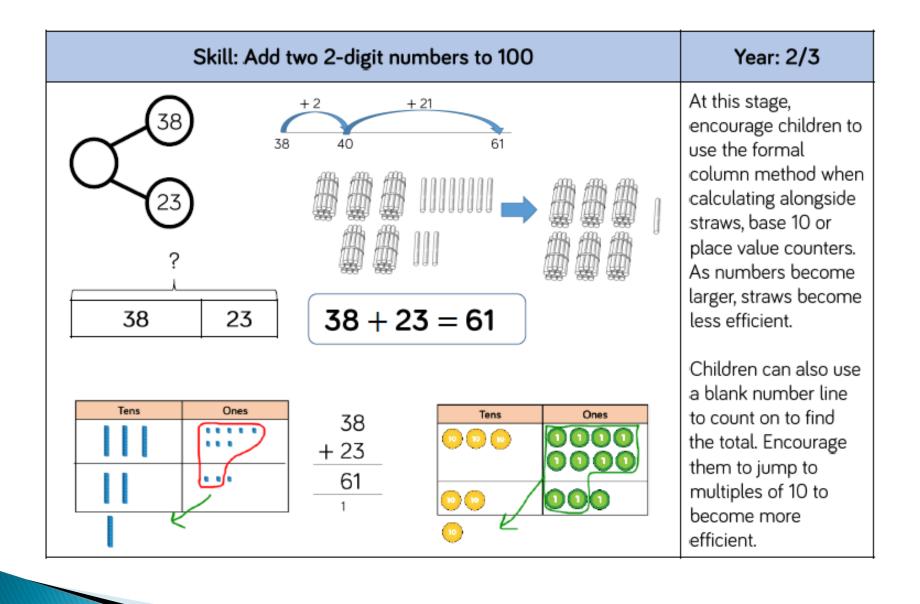
- > Add and subtract numbers mentally, including:
 - a three digit number and ones
 - a three digit number and tens
 - a three digit number and hundreds

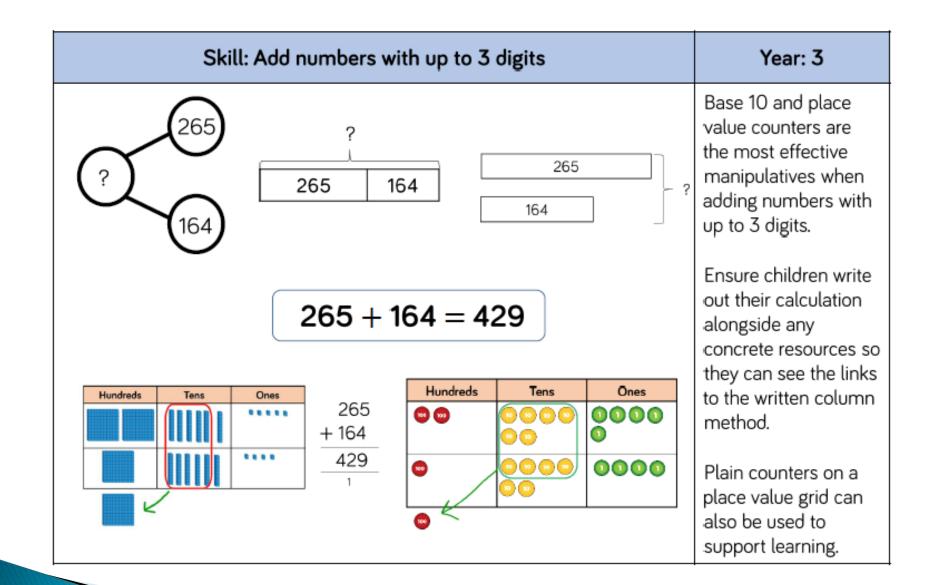
- > Add and subtract numbers with up to three digits, using formal written methods of columnar addition and subtraction.
- Estimate the answer to a calculation and use inverse operations to check answers. E.g. 234+ 244, the answer will be less than 500 because 250+250= 500
- Solve problems, including missing number problems, using number facts and place

$$13 \square - 50 = 85$$

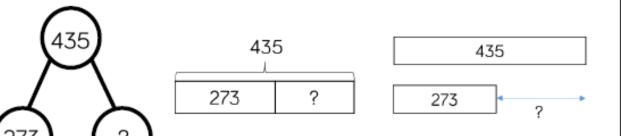
$$334 - \boxed{0} = 294$$

$$545 = 6 \boxed{5} - 70$$





Skill: Subtract numbers with up to 3 digits



$$435 - 273 = 262$$

Hundreds	Tens	Ones
		.7/1

	435
_	273
	262

マ 1

Hundreds	Tens	Ones
0000	000	00ØØ
		Ø
Ι (,	ooodd	
)	33333	
	BABABA	

e 10 and pla

Year: 3

Base 10 and place value counters are the most effective manipulative when subtracting numbers with up to 3 digits.

Ensure children write out their calculation alongside any concrete resources so they can see the links to the written column method.

Plain counters on a place value grid can also be used to support learning.

Year 4

+ 2094

- Add and subtract numbers with up to 4 digits using the formal written methods of columnar addition and subtraction
 8389
 7425
- > where appropriate.

Estimate the answer to a calculation and use inverse operations to check answers.

E.g. 1234+1244, the answer will be less than 2500 because 1250+1250=2500.

6773

Solve addition and subtraction two-step problems in contexts, deciding which operations and methods to use and why.



He buys a scooter for £345 and a skateboard for £110

How much money does he have left?

Show 3 different methods of finding the answer.

Explain how you completed each one.

Which is the most effective method?

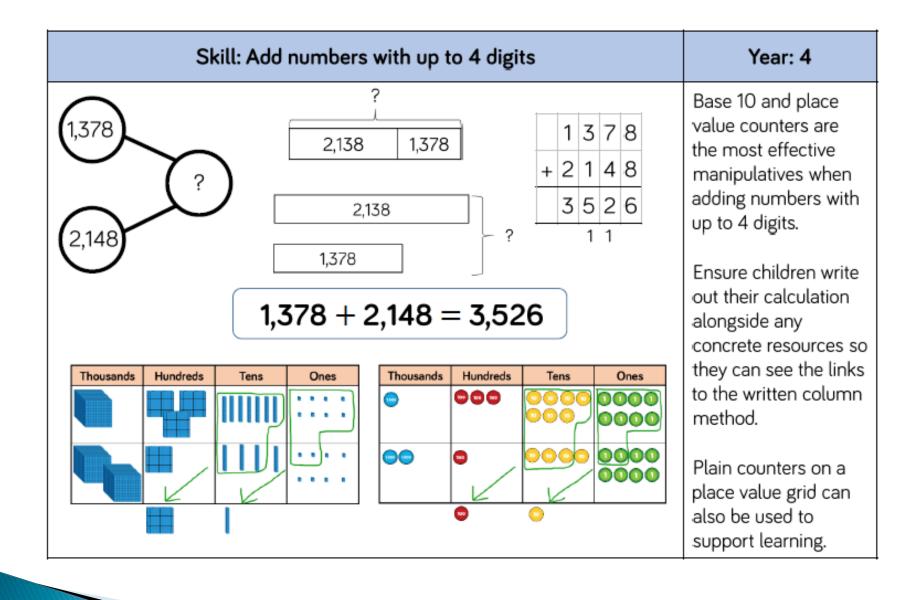
There were 2,114 visitors to the museum on Saturday.

650 more people visited the museum on Saturday than on Sunday.

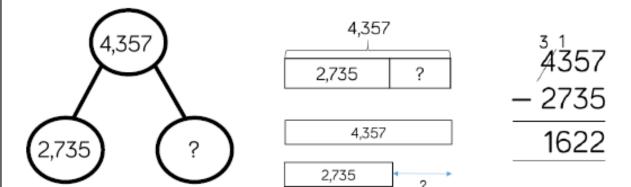


Altogether how many people visited the museum over the two days?

What do you need to do first to solve this problem?







$$4,357 - 2,735 = 1,622$$

Thousands	Hundreds	Tens	Ones
		11444	111
X			

Thousands	Hundreds	Tens	Ones
000	000 0000 0000	00 Ø Ø Ø	0000 ØØØ

Year: 4

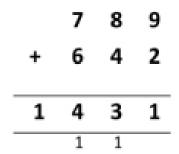
Base 10 and place value counters are the most effective manipulatives when subtracting numbers with up to 4 digits.

Ensure children write out their calculation alongside any concrete resources so they can see the links to the written column method.

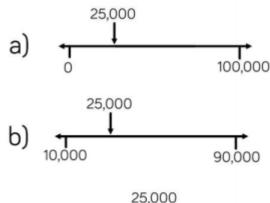
Plain counters on a place value grid can also be used to support learning.

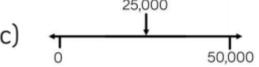
Year 5

- Add and subtract whole numbers with no more than 4 digits, including using formal written methods (columnar addition and subtraction)
- Use rounding to check answers to calculations and determine, in the context of a problem.



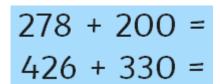
Which estimate is inaccurate?

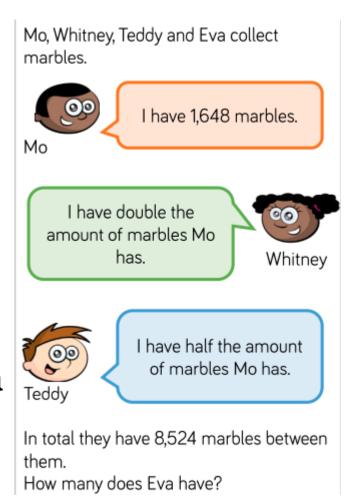


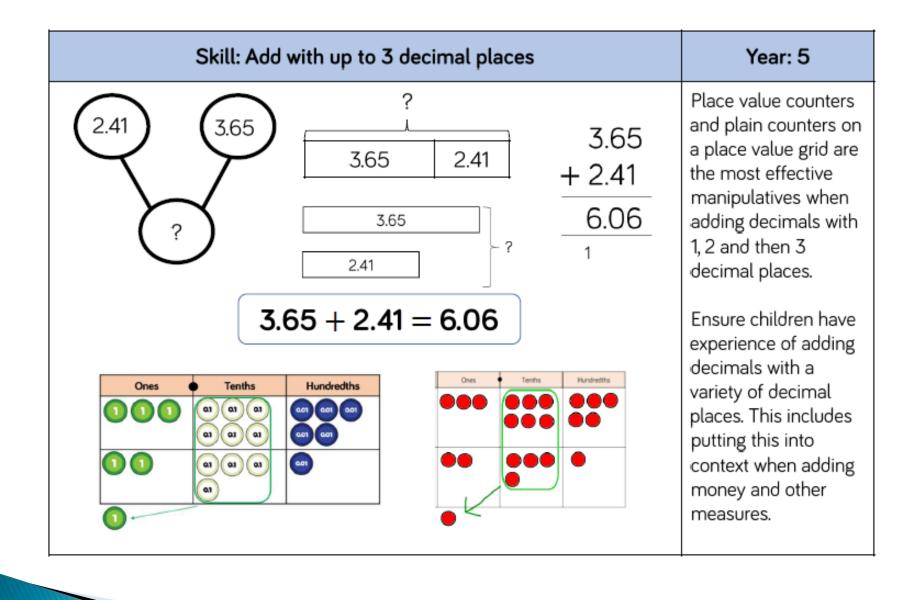


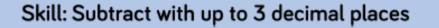
Explain how you know.

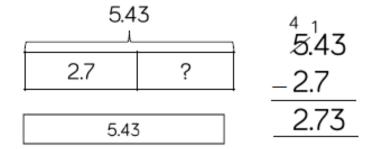
- Add and subtract numbers mentally with increasingly large numbers.
- Solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why.
- Solve problems involving addition, subtraction, multiplication and division and a combination of these, including understanding the meaning of the equals sign.











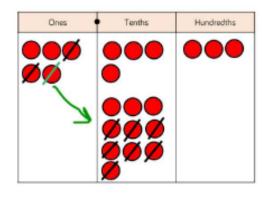
?

$$5.43 - 2.7 = 2.73$$

2.7

Ones •	Tenths	Hundredths
0000	(1) (1) (1)	0.01 0.01
0	00000	

5.43



Year: 5

Place value counters and plain counters on a place value grid are the most effective manipulative when subtracting decimals with 1, 2 and then 3 decimal places.

Ensure children have experience of subtracting decimals with a variety of decimal places. This includes putting this into context when subtracting money and other measures.

 Solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why.

A milkman has 250 bottles of milk.

He collects another 160 from the dairy, and delivers 375 during the day.

How many does he have left?



My method:

$$375 - 250 = 125$$

$$125 + 160 = 285$$

Do you agree with Tommy? Explain why.

On Monday, Whitney was paid £114

On Tuesday, she was paid £27 more than on Monday.

On Wednesday, she was paid £27 less than on Monday.

How much was Whitney paid in total?

How many calculations did you do?

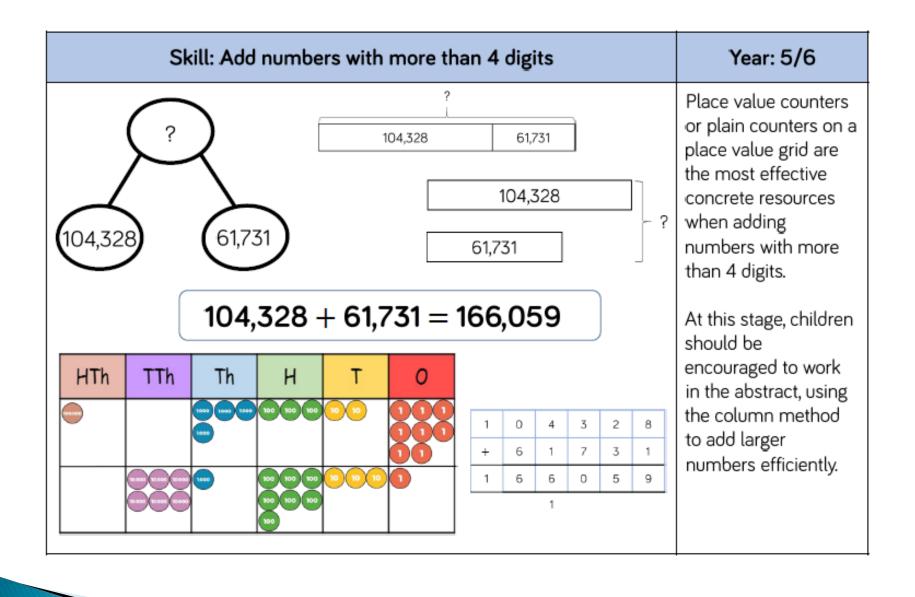
Is there a more efficient method?

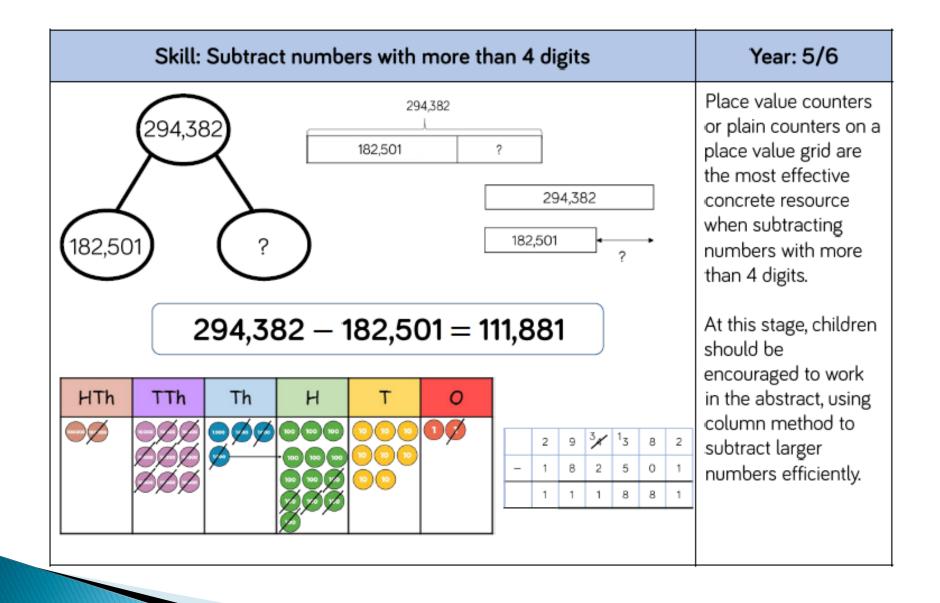
- Perform mental calculations. Including with mixed operations and large numbers.
- Use their knowledge of the order of operations to carry out calculations involving the four operations.

Order of Operations

В	Brackets	10 × (4 + 2) = 10 × 6 = 60
I	Indices	5 + 22 = 5 + 4 = 9
D	Division	10 + 6 ÷ 2 = 10 + 3 = 13
M	Multiplication	10 - 4 × 2 = 10 - 8 = 2
A	Addition	10 × 4 + 7 = 40 + 7 = 47
S	Subtraction	10 ÷ 2 - 3 = 5 - 3 = 2

$$(19-7) + 8^2 + 9 =$$





Websites

- Gov website Mathematics National Curriculum
- ➤ St Catherine's website ⇒ learning ⇒ Maths
- Maths, Calculation and Addition/subtraction policies
- White Rose Schemes of Learning
- ➤ whiterosemaths.com⇒ resources ⇒ primary resources
- NCETM
- oxfordowl.co.uk

Maths Games

- https://home.oxfordowl.co.uk/kids-activities/fun-mathsgames-andactivities/www.bbc.co.uk/cbeebies/topics/numeracy
- Nrich
- > BBC Bitesize
- Board games Yahtzee, Rummikub, snakes and ladders, Monopoly, Bingo, Dominoes
- Dice games
- Card games: 10 pairs (addition/number bonds), Snap (cards add up to target number) etc
- Math Boggle (16 number cards make a maths sentence) Topmarks.co.uk
- Hit the button- Number bonds and times tables
- education.com/games/math/
- uk.splashlearn.com/place-value-games
- www.ictgames.com/mobilePage/placeValue

mathsbot.com/manipulativeMenu

Questions

